

VEER NARMAD SOUTH GUJARAT UNIVERSITY, SURAT

M.Sc. Industrial Mathematics

Scheme of teaching and examination

Semester – I

Subject Code	Subject	Scheme Of Teaching			Scheme Of Examination					
		L	P	Total	Th.		Pr.		Total	
					Int	ext	Int	Ext	Int	Ext
IM – 101	Real Analysis	4	--	4	30	70	--	--	30	70
IM – 102	Ordinary Differential Equations	4	--	4	30	70	--	--	30	70
IM – 103	Linear Algebra	4	--	4	30	70	--	--	30	70
IM – 104	Advanced Numerical Techniques	4	--	4	30	70	--	--	30	70
IM – 105	Mechanics	4	--	4	30	70	--	--	30	70
IM – 106	Programming Language	4	4	8	18	42	12	28	30	70
	Total	24	04	28	168	392	12	28	180	420

Semester – II

Subject Code	Subject	Scheme Of Teaching			Scheme Of Examination					
		L	P	Total	Th.		Pr.		Total	
					Int	ext	Int	Ext	Int	Ext
IM – 201	Complex Analysis	4	--	4	30	70	--	--	30	70
IM – 202	Partial Differential Equations	4	--	4	30	70	--	--	30	70
IM – 203	Functional Analysis	4	--	4	30	70	--	--	30	70
IM – 204	Numerical Linear Algebra	4	--	4	30	70	--	--	30	70
IM – 205	Design and Analysis of Algorithm	4	--	4	30	70	--	--	30	70
IM – 206	Object Oriented Programming with C++	4	4	8	18	42	12	28	30	70
	Total	24	04	28	168	392	12	28	180	420

Semester – III

Subject Code	Subject	Scheme Of Teaching			Scheme Of Examination					
		L	P	Total	Th.		Pr.		Total	
					Int	ext	Int	Ext	Int	Ext
IM – 301	Applied Statistics	4	--	4	30	70	--	--	30	70
IM – 302	Integral Equation	4	--	4	30	70	--	--	30	70
IM – 303	Optimization	4	--	4	30	70	--	--	30	70
IM – 304	Fluid Dynamics	4	--	4	30	70	--	--	30	70
IM – 305	Modeling and Simulation	4	--	4	30	70	--	--	30	70
IM – 306	File Organization and Database Systems	4	4	8	18	42	12	28	30	70
	Total	24	04	28	168	392	12	28	180	420

Semester – IV

Subject Code	Subject	Scheme Of Teaching			Scheme Of Examination					
		L	P	Total	Th.		Pr.		Total	
					Int	ext	Int	Ext	Int	Ext
IM – 401	Image Processing	4	--	4	30	70	--	--	30	70
IM – 402	Wavelet Analysis	4	--	4	30	70	--	--	30	70
IM – 403	Digital Signal Processing	4	--	4	30	70	--	--	30	70
IM – 404	Computational Fluid Dynamics	4	--	4	30	70	--	--	30	70
IM – 405	Neural Network	4	--	4	30	70	--	--	30	70
IM – 406	Mathematical Software	4	4	8	18	42	12	28	30	70
	Total	24	04	28	168	392	12	28	180	420

IM 1 01: Real Analysis

Syllabus to be offered at M. Sc. Industrial Mathematics Sem - I w.e.f. June 2010-11

L	T	P
4	1	0

Prerequisite

The extended real numbers, sequences of real numbers, open and closed sets of real numbers axioms for the real number, continuous functions, borel sets.

Lebesgue measure

Introduction, outer measure, measurable sets and lebesgue measure, non measurable sets, measurable function, littlewood's three principles.

Lebesgue integral

Riemann integral, lebesgue integral of a bounded function over a set of finite measure, integral of a non negative function, general lebesgue integral

Differentiation and integration

Differentiation of monotone functions, functions of a bounded variation, Differentiation of an integral, absolute continuity, convex functions.

Measure and integration

Measures spaces, measurable functions, integrations, general convergence theorem, signed measures, the Random – Nikodym theorem. The L^p – Spaces.

Measures and outer Measures

Outer measures and measurability, the extension theorem, the lebesgue Stieltjes iintegral, Product measure, integral operators, caratheodory outer measure, hausdroff measure

References:

1. H. L. Royden, Real Analysis, Macmillan publication, 1993.
2. Walter Rudin, Principles of mathematical analysis, McGraw Hill, 1976.
3. T. M Apostol, Mathematical Analysis, Narosa publishing house ,1985.
4. G.de. Barra, Measure theory and Integration, Wiley Eastern limited,1981.
5. I. P. Natanson, Theory of Functions of real variable,Fredrick Unger pub.1961.

IM 102: Ordinary Differential Equations

Syllabus to be offered at M. Sc. Industrial Mathematics Sem - I w.e.f. June 2010-11

L	T	P
4	1	0

- Mathematical modeling by means of ordinary differential equations
- Reduction of nth order equation into first order systems
- Existence and uniqueness of solution of a nonlinear system of ordinary differential equations, Lipschitz condition, Gronwall's lemma.
- Phase plane Analysis
- Linearization of nonlinear systems
- Autonomus and nonautonomus Linear system Theory: Linear Dependence and independence of solution, Wronskian.
- Transition matrix(fundamental matrix) for a linear system, solution of a nonlinear system by variation of parameters method, computation of transition matrix , eigenvalue method, Peano-Backer series method.
- Discrete dynamical systems
- Stability of dynamical systems, Lyapunov, exponential and asymptotic stability and their characterization.
- Sturm -Liouville equations, Eigenvalue problems
- Series solution of non-autonomous systems, Bessel and Legendre series, Frobenius method.

.Reference Books:

1. S.L. Ross: Differential equations, Blaisdell publishing company, First edition, 1964
2. Birkhoff G and Rota G.C.: Ordinary differential equations, Boston, 1962
3. Coddington E. A and N. Levinson: Theory of ordinary differential equations, McGraw-Hill, New York, 1955.
4. Saber N. Elaydi: An introduction to Differential Equations, Springer-verlag, Second edition, 1995
- 5.V.I. Arnold: Ordinary Differential Equations, Prentice- Hall of India,

IM 103: Linear Algebra

Syllabus to be offered at M. Sc. Industrial Mathematics Sem - I w.e.f. June 2010-11

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Linear operator

Functions linear operators, null space and range, rank and nullity theorem, operator inverses, application to matrix theory, computation of null space and range of a matrix, matrix of an operator, change of basis and similar matrices.

Inner product spaces

Basics of inner product space, orthogonal sets fourier coefficients and partial identity gram-schmidt process QR factorization, approximation and orthogonal projection, equivalence of the problems, normal equations projection operators, orthogonal complements, applications to an approximations and matrix theory fredholm alternative theory, matrix representation of an inner products, orthogonal change of bases, rank of gram matrix

Diagonalizable linear operators

eigen values and eigen vectors, spectrum and eigen spaces of an operator, thortical computation using determents, property of the characteristic polynomial, geometric and algebraic multiplicity, diagonalizable operator and their computational advantages, similarity to a diagonal matrix, function of a diagonalizable operator, function of matrices, general properties of function of diagonalization operator, miniaul polynomial, first order matrix differential operator, decoupling the differential eauation, estimates of eigen values, gershgorin's theorem

References:

1. J. T. scheick, Linear algebra with application, McGraw - Hill international addition, 1997.
2. S. Biswas, Matrix Algebra, new age int. pub. 2nd ed. 1997
3. A. R. Rao & P. Bhima Shankaram, Linear Algebra, Tata McGraw Hill New Delhi – 1996

IM 104: Advanced Numerical Techniques

Syllabus to be offered at M. Sc. Industrial Mathematics Sem - I w.e.f. June 2010-11

L	T	P
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- Computer Arithmetic: Floating point numbers and round off errors, Absolute and relative errors.
- Polynomial Interpolation: Hermite's interpolation formula with error analysis, Richardson interpolation, splines and spline interpolation, Aitken extrapolation
- Numerical differentiation, Gaussian quadrature, Romberg integration, adaptive quadrature
- Solution of system of Linear equations:
 - Matrix inversion, Jordan's method, Escalator method and iterative method.
 - The LU and Cholesky factorizations
 - Pivoting and constructing an algorithm based on Gaussian elimination method
 - Solution of equations by iterative methods (Jacobi's method, Gauss-Seidel method)
 - Steepest descent and Conjugate gradient methods.
- Algebraic Eigen value problem :
- Properties of eigen values and eigen vectors
- Power method
- Inverse power method
- Jacobi's method, Given's method
- Schur and Gershgorins theorem
- Orthogonal factorization
- QR algorithm for eigen value problem
- Eigen values of complex matrix and complex eigen vectors
- Approximation:
Different types of approximation, Least square polynomial approximation, Polynomial approximation by use of orthogonal polynomials, approximation with Chebyshev polynomials.
- Numerical Solution of ODE: single step method-Runge Kutta methods, Multistep method - Milne Simpson's method.
- System of non linear equations: Newton Raphson's method

Reference Books:

1. C.E. Froberg: Introduction to Numerical Analysis, Addison Wesley publishing Company, sixth edition, 1981.
2. S.S. Sastri: Introductory Methods of Numerical Analysis, Prentice Hall of India, New Delhi, 1997.
3. E.V. Krishnamurthy and S.K.Sen: Computer based numerical Algorithms, East – West press Pvt. Ltd. 1976
4. Conte S.D and Carl deBoor: Elementary Numerical Analysis: an algorithmic approach, Mc Graw Hill company, Third edition, 1981
5. M.K. Jain: Numerical analysis for scientists and Engineers, New Age International Ltd. Publishing, 1992

IM 105: Mechanics

Syllabus to be offered at M. Sc. Industrial Mathematics Sem - I w.e.f. June 2010-11

L	T	P
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FUNDAMENTALS OF PHYSICS

- Measurement
- Motion in one dimension: Displacement, Velocity, Acceleration, Equation of motion with constant acceleration.
- Motion in two dimension and three dimensions: Displacement, Velocity, Acceleration, Projectile Motion, Uniform circular motion, Relative motion in two and three dimension
- Newton Laws of motion (with examples), Friction and centripetal forces
- Kinetic energy and work ,Work done by weight, Work done by variable force, Work-kinetic energy theorem, Work done by spring force, Power, Potential energy and conservation of energy, Electric potential energy, Gravitational potential energy, Conservation of energy
- System of particles: Newton Laws for system of particle, Linear Momentum and Newton's second Law, Conservation of linear momentum, collision, Impulse and linear momentum, Elastic and Inelastic collision in one dimension, Collision in two dimension
- Rotational motion: Angular displacement, Angular velocity and Angular acceleration, Equation of motion for constant angular acceleration, Torque, Newton second law in angular form
- Elasticity
- Planets and satellites: Kepler's law
- **Oscillations and wave theory**
- Oscillations: Energy, SHM, Energy in SHM, damped simple harmonic motion, forced oscillations and resonance, Simple pendulum
- Waves: Types of waves, wavelength, frequency, period, angular frequency, Superposition of waves
- Sound waves: Doppler effect
- **Heat and Thermodynamics**
 - Thermodynamics : Zeroth Law of Thermodynamics
 - The Celsius, Kelvin and Fahrenheit scales

- Thermal expansion: Linear expansion and volume expansion
- Specific heat
- First law of Thermodynamics
- Conduction, convection, radiation
- Kinetic theory of Gases and second law of Thermodynamics: Ideal gases, Internal energy, the Adiabatic expansion of an ideal gases, Entropy, Second law of thermodynamics, Entropy in the real world, Engines, Refrigerators
- **Electromagnetism**
 - Electric charge, Conductors and insulators, Coulomb's law.
 - Electric field, Electric field due to a point charges, Electric field due to an electric dipole, Gauss law.
 - Electric Potential, Equi-potential surfaces, Calculation of Potential from field, Potential due to a point charge
 - Capacitors, Capacitance, Capacitors in series and parallel, Capacitor with a Dielectrics.
 - Moving charges and electricity, Currents, Semi conductors, Super conductors., Electric current, Current density, Resistance and Resistivity, Ohms law.
 - Circuits: Work, energy, emf, power, Ameter and voltmeter, RC circuits, Kirchoff's law
 - The Magnetic field, definition of B, Hall effect, Torque on a current loop, Magnetic dipole.
 - Magnetic field due to current, Amperes law, solenoids.
 - Faraday's law, Lenz's law, Inductance and inductors, self inductance, RL circuits, energy stored in magnetic fields
 - Maxwell's equations: magnetic moments, magnates, Paramagnetism, diamagnetism, ferromagnetism, Maxwell's equations
 - Geometric optics : Plane mirrors, spherical mirrors, thin lenses
 - Wave optics : Interference and diffraction .

Reference Books:

1. D. Halliday, R. Resnick and J. Walker, Fundamentals of Physics, Sixth edition, John Wiley and Sons, New York, 1998.
2. J.B. Serway, Fundamental of Physics

IM 106: Programming Language

Syllabus to be offered at M. Sc. Industrial Mathematics Sem - I w.e.f. June 2010-11

L	T	P
4	1	4

Introduction

Algorithms and Flowchart, Types of Languages, Introduction to C Language

C Fundamentals

Identifiers, Data Types, Constants and Variables, Arrays

Operators and Expressions

Arithmetic Operators, Unary Operators, Relations Operators, Logical Operators
Assignment Operators, Conditional Operators, Library Functions, Expressions, Evaluation of
Expression

Data Input and Output

Single Character input and output, The scanf function, The printf function, Gets and Puts
functions

Control statements

The While Statement, do-while statement, for statement, if – else statement, switch
statement, break statement, continue statement, goto statement

Functions

Introduction to functions, Function definition, Accessing function, Passing arguments to
function, Recursive function

Arrays

Defining an array, Processing an array, Multi dimensional arrays, Passing array to a
function, Arrays and Strings

Structures and Unions

Defining a structure, Processing a structure, Unions

Reference Books

1. C programming Language – karnighan & Ritchie – TMH
2. 'C' Odyssey 6th Volume – Vijay Mukhi – PHI
3. Programming in 'C' – Stephan Kochan – CBS
4. Mastering turbo C- Kelly and Bootle – BPB
5. C language Programming Byron Gottfried – TMH

IM 201: Complex Analysis

Syllabus to be offered at M. Sc. Industrial Mathematics Sem - II w.e.f. June 2010-11

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Basic of complex Numbers:

Analytic Functions:

Functions, limits and continuity, differentiability Power series as an analytic function, Exponential and Trigonometric functions, Complex logarithms, Inverse functions, Zeros of analytic functions.

Complex Integration:

Curves in the complex plane, Basic properties of complex Integral, winding number or index of a curve, Cauchy-Goursat Theorem, Homotopy version of Cauchy's theorem, Morera's theorem, Cauchy Integral Formula, Laurent series, The maximum modulus principle, Schwarz's lemma, Liouville's theorem.

Singularities:

Isolated and non-isolated singularities, removable singularities poles, singularities at infinity, Analytic continuations.

Residues and evaluation of certain integrals:

Residue at a finite point, residue at a point at infinity, residue theorem, no of zeros and poles, Rouché's theorem, integrals of type $\int_{\alpha}^{2\pi+\alpha} R(\cos \theta, \sin \theta) d\theta$, integrals of type $\int_{-\infty}^{\infty} f(x) dx$, integrals of type $\int_{-\infty}^{\infty} g(x) \cos(mx) dx$, singularity in real axes, more on using rectangular curves, estimation of sums

References:

1. S. Ponnuswamy, foundation of complex analysis, Narosa publishing house, 1997.
2. S. Lang, Complex Analysis, Addison Wesley, 1997.
3. J. N. Sharma, Functions of a Complex Variable, Krishna Prakashan, 2000.
4. H. A. Priestly, introduction to complex analysis, Clarendon Press, 1990.
5. J. B. Conway, Functions of one complex variable, Springer- verlag, 1980.

IM 202: Partial Differential Equations

Syllabus to be offered at M. Sc. Industrial Mathematics Sem - II w.e.f. June 2010-11

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- Introduction to PDE, Modelling Problems related to PDE.
- General PDE, Classification of PDE -hyperbolic, elliptic and parabolic PDE
- Boundary conditions, well-posed problem, The Cauchy-Kowalewski theorem for existence and uniqueness of solutions to PDE
- **Hyperbolic PDE**
 - Scalar first order Partial differential equations, Characteristics, Charpits method, Weak Solutions., Quasi-linear first order equations and quasi-Linear systems of partial differential equations, weak solutions, shocks and rerefactions, Burgers equation, non-uniqueness and entropy conditions, Wave equation
- **Elliptic PDE**
 - Solution of Laplace equation using separable variable technique, Fundamental solution, Mean value theorem., Strong Maximum Principle, uniqueness and regularity, Energy Methods, Sobolev spaces and Lax-Milgram lemma.
- **Parabolic PDE**
 - Solution of Heat equation using Fourier Transform method, Mean Value Theorem, Maximum Principle, Regularity, Uniqueness, Semigroup approach

Reference Books:

1. Strauss W. A: Partial differential equations, An Introduction, Wiley, John and sons 1992.
2. Renardy and Rogers: An introduction to PDE's, Springer-Verlag, 1999.
3. Smoller: Shock Waves and reaction-diffusion equations, second edition, 1994.
4. Kevorkian: Partial Differential equations, Wadsworth and Brooks/ cole
5. F.John: Partial differential equations

IM 203: Functional Analysis

Syllabus to be offered at M. Sc. Industrial Mathematics Sem - II w.e.f. June 2010-11

L	T	P
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Metric Spaces

Metric space, Examples of Metric Space, Open sets, Closed sets, Neighborhood, Convergence, Cauchy sequence, Completeness, Completion of metric space.

Normed Spaces and Banach Spaces

Vector Space, Normed Space, Banach Space, Properties of Normed spaces, Finite Dimensional normed space and subspaces, Compactness and finite dimension, Linear operators, Bounded and continuous linear operators, Linear functionals, Linear operators and functionals on a Finite dimensional spaces, Normed spaces of operators, Dual spaces

Inner Product Spaces, Hilbert Spaces

Inner Product space, Hilbert space, Properties of Inner product Space, Orthogonal complements and direct sums, Orthonormal sets and sequences, Series related to orthonormal sequences and sets, Total orthonormal sets and sequences, Representation of functionals on Hilbert spaces, Hilbert adjoint operator, Self adjoint unitary and normal operator.

Fundamental theorems for Normed and Banach spaces

Zorn's Lemma, Hahn – Banach theorem, Hahn – Banach theorem for complex vector spaces and normed spaces, applications to Bounded linear functionals on $C[a, b]$, Adjoint operator, Reflexive spaces, Category theorem and uniform boundedness theorem, Strong and weak convergence, Convergence of sequences of operators and functionals, Weak convergence, Open mapping theorem, Closed linear operators, Closed Graph theorem.

References:

1. E. Kreyszig: Functional Analysis and its application, John Wiley and sons.
2. B.V. Limaye : Functional Analysis, Wiley Eastern Ltd.
3. G.F. Simmons : Introduction to Topology and Modern Analysis, McGraw - Hill.
4. J.N. Sharma & A Vashistha :Functional Analysis.

IM 204: Numerical Linear Algebra

Syllabus to be offered at M. Sc. Industrial Mathematics Sem - II w.e.f. June 2010-11

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Vector and Matrix Norms:

Vector Norms, Matrix Norms, Convergent Matrices, Stability of Nonlinear Systems,

Iterative Methods and Condition Number

Introduction, Gauss-Jacobi Iteration Method, Gauss-Seidel Iteration Method, Convergence of Iteration Methods, Successive Over-Relaxation Iteration Method, Conjugate Gradient Method, Definition and Examples, Elementary Properties of $k(A)$, Sensitivity Analysis of Solutions of Linear Systems, Residual Theorem, Nearness to Singularity, Estimating $k(A)$,

Singular Value Decomposition

SVD Theorem, Algebraic and Geometric Properties of SVD, Determining the Rank of a Matrix Using SVD, Compression Using SVD, Pseudoinverse and the SVD,

Numerical Eigenvalue Problem

Basic Theorem on Eigenvalues and Eigenvectors, Power Method, Power Method Algorithm, Rate of Convergence, Power Method with shift, Simple application of power method with shift, Calculating the least Dominant Eigenpair, Inverse Iteration, Rayleigh Quotient, Householder Deflation, Jacobi's Method, Rotation Matrices, The Outline of Jacobi's Method, The General Step of Jacobi's Method, Zeroing out d_{pq} and d_{qp} , QR Method, Hessenberg QR Method, Rate of Convergence of the hessenberg QR Method, Single Shift Hessenberg QR Method.

References:

1. V. Sundarapandian : Numerical Linear Algebra, P.H.I. New Delhi, 2008.
2. Bretscher O. : Linear Algebra with applications Prentice Hall, Englewood Cliffs, New Jersey, 1997.
3. Ciarlet P.G. : Introduction to Numerical Linear Algebra and Optimization, Cambridge University Press, Cambridge, 1989.
4. Cullen C.G.: An Introduction to Numerical Linear Algebra, PWS Publishing Company, Boston, 1994.
5. Datta B.N. : Numerical Liner Algebra, Brooks and Cole, Pacific Grove, 1995.
6. Demmel J.W. : Applied Numerical Linear Algebra, SIAM, Philadelphia, 1997.
7. Hager W.W.: Applied Numerical Linear Algebra, Prentice Hall, Englewood Cliffs, New Jersey, 1988.
8. Loan C.F.V.: Introduction to Scientific Computing, Prentice Hall, Englewood Cliffs, New Jersey, 2000.
9. Trefethen L.N. and D. Bau : Numerical Linear Algebra, SIAM, Philadelphia, 1997.

IM 205: Design & analysis of Algorithm

Syllabus to be offered at M. Sc. Industrial Mathematics Sem - II w.e.f. June 2010-11

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- Logic

Propositional and predicate logic, propositions, predicates and quantifiers, quantifier and logical operators, rules of inference, methods of proof and logical verification of computer programs.

- Theory of algorithms

Problems and instances algorithms, characteristics of algorithms, concepts of test data, efficiency of algorithms, theoretical, empirical and hybrid approaches to measure efficiency, time complexity, space complexity, asymptotic notations, solving recurrences using characteristics equations, examples of simple algorithm and their analysis

- Graph theoretic algorithms and computer programs

Recap the concepts and definitions of graph and trees as data structure , some basic algorithms, representation of graphs, breath first search, topological search, heap sort algorithm connectedness and assumptions, Lattice theory, Boolean algebra

- Theory of Computation

Models in computer science, finite state automata, their use and properties, Deterministic finite automata, non deterministic finite automata, regular languages and their unions, finite state transducers, Push down automata, context free languages, turning machine and computing by turing machines.

References:

1.Harry R. Lewis and Christosh H. Papadimitriou.

Elements of the theory of computation, Prentice Hall of India. 1996

2.V.Aho,J.E.Hoperoft and J.D. Vilman

The design and analysis of Computer algorithms. 1974

3.Thomas H. Cormen Leiserson and Rivest

Introduction to algorithm, Prentice Hall of India, 1998

4.Dino Mandrioli, Carlo Ghezzi : Theoretical foundations of computer science,

John-Wiley and sons, 1987

IM 206: Object Oriented Programming

With C++

Syllabus to be offered at M. Sc. Industrial Mathematics Sem - II w.e.f. June 2010-11

L	T	P
4	1	4

Principles of object oriented Programming

Procedure oriented Programming Vs object Oriented Programming, Benefits of Object oriented Programming

Classes and Objects

Constructions and Destructions

Operators Overloading, Functional Overloading and Type Conversions.

Inheritance

Pointers

Basis of Pointers, Pointer Arithmetic, Pointer Array, Call by reference in user defined functions, Pointer to function

Files:

Reading and writing from a file, Reading and writing Structures, Random acceseing a file

References:

1. R. Decker and S.Hirshfield (1998) : The Object Concept: An Introduction to Computer Programming using C++ , PWS Publishing.
2. S.B.Lippmann and J.Lajoie (1998) : C++ Primer , Third Ed., Addison Wesley.
3. W.J. Savitch (2001): Problem Solving with C++ : The Object of Programming. Third Ed., Addison Wesley.

IM 301: Applied Statistics

Syllabus to be offered at M. Sc. Industrial Mathematics Sem -III w.e.f. June 2011-12

L	T	P
4	1	0

- **Probability :**

Basic concepts, Sample space, Discrete probability ,Simple theorems on probability, Independence of events, Bayes theorem. Discrete and continuous random variable, Binomial, Poisson and Normal distributions, expectation and moments, Chebyshev's inequality, central limit theorem.

- **Statistics:**

Data analysis , measures of central tendency, measures of dispersions, curve fitting, regression, correlation, chi-square test of goodness of fit, contingency tables, confidence interval for mean , variance. One population case, two population case, testing of hypotheses, small samples and large samples, sampling techniques, Simple random sampling with and without replacement, stratified sampling.

control charts for variables and attributes, acceptance sampling by attributes, simple, double and sequential sampling plans, Design of experiments

Stochastic processes:

Markov chains with finite and countable state space, classification of states, limiting behavior of n-step transition probabilities, Continuous Markov process.

References:

1. Berry and Lindgren: Statistics theory and methods , second edition, Duxburg, Boston, 1996
2. Hastings: Probability and statistics, Addison Wesley Longman, Boston, 1997.
3. Hogg and Tannis: Probability and Statistical inference, sixth edition, Prentice- Hall, Upper Saddle River, New Jersey, 2000
- 4 S.C.Gupta and V.K. Kapoor: Fundamentals of Mathematical Statistics, Sultan chand and sons, 2000
5. S.,P.Gorden and F.S. Gorden: Contemporary Statistics, a computer approach, 1994

IM 302: Integral equations

Syllabus to be offered at M. Sc. Industrial Mathematics Sem -III w.e.f. June 2011-12

L	T	P
4	1	0

Variational problems with fixed boundary

The concepts of variational parameter, and its properties, variational forms of functional form, function depends on Higher order derivatives, functionals dependent on function of several independent variables, variational problem in parametric forms, application to the problems of mechanics, variational problems leading to an integral equation or differential difference equations, theorem of Dubois' Reymond stochastic calculus of variation,

Variational problem with moving boundary

Functional of the form $I(y(x)) = \int_{x_1}^{x_2} F(x, y, y') dx$, variational problem with a moveable boundary

for a functional dependent on two function, one sided variation, reflection and refraction of extremals, diffraction of light rays

Variational problem with subsidiary conditions

Constrains of the form, isoperimetric problems, problems of Mayer & Bolza, equilibrium problem for elastic bodies- castigliano's principle, problems of electro static

References:

1. A. S. Gupta, calculus of variation with applications, prentice-hall India, 1997.
2. J. David Logan, applied mathematics, john wiley and sons, 1997.

IM 303: Optimization

Syllabus to be offered at M. Sc. Industrial Mathematics Sem -III w.e.f. June 2011-12

L	T	P
4	1	0

- Optimization problems in engineering and industries
- Optimization problem formulation
- Classification of optimization problem
- Classical optimization techniques : Single variable optimization, Multivariable optimization, Constraint optimization, Lagrangian multiplier method, Kuhn-Tucker conditions
- Single variable optimization techniques:
 - Bracketing method - Exhaust search
 - Region elimination method - Interval halving method, Golden section method
 - Interpolation method - Quadratic interpolation method
 - Gradient base methods - Newton-Raphson method, bisection method
- Multivariable optimization techniques:
 - Univariate method
 - Direct Search method - Simplex search method, Powells conjugate direction method
 - Gradient base methods - steepest descent method, conjugate gradient method
 - Variable matrix method
- Constraint linear optimization problem
- Overview of linear optimization problem
- Sensitivity analysis
- Quadratic programming - Wolf's modified simplex method, Bailes methods
- Integer programming problem - Gomory's cutting plane method, branch and bound techniques

References:

1. Kantiswarup, P.K.Gupta and Manmohan: Operations Research ,Sultan chand and Sons.
2. S.D. Sharma: Operations Research, Kedar Nath, Ram Nath & Co.
3. S. S. Rao: Optimization Theory and Applications, Wiley Eastern, 1984
4. B.E. Gillet : Introduction to Operation Research Computer Oriented algorithm

IM 304: Fluid Dynamics

Syllabus to be offered at M. Sc. Industrial Mathematics Sem -III w.e.f. June 2011-12

L	T	P
4	1	0

- Vectors and Tensors:
- Flow Kinematics
- Flow descriptions (Lagrangian, Eulerian, Material derivative)
- Motion of Fluid particles(rate of dilation, rate of shear, rate of rotation)
- Conservation Laws
- Reynold's transport theorem
- Conservation of mass
- Conservation of momentum
- Conservation of energy
- Navier-stokes equation
- Non dimensionalization of the Navier-stokes equation
- Special form of conservation laws
- Euler equation for inviscid gas dynamics
- Parabolic boundary condition for N S equation
- Vorticity and Circulation
- The vorticity transport equation and Helmholtz's vorticity.
- Kelvin's circulation theorem.
- Potential equation
- Laplace Equation for irrotational flows
- Incompressible inviscid irrotational flows
- Velocity potential and stream function in 2d and 3d
- Complex velocity potential
- Simple planer flows
- Incompressible Viscous flows
- Boundary layer equations

References:

1. Batchelor G.K.: An Introduction to Fluid Dynamics, Cambridge University Press,1999.
2. Emanuel G: Analytical Fluid Dynamics, CRC Press, Boca Raton, Second Edition, FL, 1999.
3. Panton R.L., Incompressible Flows, Wiley Interscience, 1984
4. Currie I.G.: Fundamental Mechanics of Fluids, McGraw-Hill, New-york, 1993.
5. Chorin: Mathematical introduction to Fluid Mechanics, Springer Verlag, Fourth Edition

IM 305: Modeling & Simulation

Syllabus to be offered at M. Sc. Industrial Mathematics Sem -III w.e.f. June 2011-12

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- Needs and Techniques of mathematical modeling: Idea of mathematical modeling, need for mathematical modeling, steps in mathematical modeling, Characteristics of mathematical modeling ,Interpretation
- Models in mechanical vibration :Spring mass system, pendulum problems
- Models in population dynamics:One species model, logistic model, growth model in time delays ,Predator-Prey models,Volterra-Lotka models
- Models of chemical processes, Electrical network and Diffusion processes
- Traffic flow models

COMPUTATIONAL MODELING

- Modeling dynamical systems: differential equations and their numerical solution, linear and non-linear dynamics, stability, convergence, attractors.
- Physical systems: System types and characteristics behaviour, Continuous-time,discrete – time and discrete -event systems, linear and non linear systems
- Exploration of behaviour through simulation:

Developing simulations of dynamical systems using Matlab: representation and visualization of simulation experiments, analyzing behavioural characteristics for a range of classes of physical and computational systems eg. Predictor- prey models, evolutionary systems and cellular systems

References:

1. J.N.Kapur: Mathematical modelling ,Wiley eastern Ltd.,1994.
2. M.M. Gibbons : A concrete approach to Mathematical modeling , John Wiley and sons, 1995.
3. H. Neunzert and A.H. Siddiqui: Topics in Industrial Mathematics, Kluwer Academic Publishers, London, 2000
4. P. E. Wellstead : Introduction to Physical system modeling, Academic Press, 1979.
5. Richard Haberman: Mathematical Models, Practice- Hall Inc., NJ, 1979.
6. Jery Banks, John S., Carson II, Barry Nelson and David M.Nicol,:Discrete – Event system simulation , Prentice hall, 2001

IM - 306 File Organizations and Database System

Syllabus to be offered at M. Sc. Industrial Mathematics Sem -III w.e.f. June 2011-12

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- Streams and Files
- Advantages of streams
- Stream class hierarchy
- The ios class
- The istream class
- The ostream class
- Stream errors
- Disk file I/O with stream
- File pointers
- Error handling in file
- File I/O with member function
- Overloading the extraction and insertion operators
- Memory as a stream objects
- Command line argument
- Creating Multi file programs

Reference:

1. C Programming Language - Karnighan & Ritchie - THM
2. 'C' Odyssey 6th Volume - Vijay Mukhi - PHI
3. Programming in 'C' - Stephen Kochan - CBS
4. Mastering Turbo C - Kelly and Bootle - BPS
5. C language Programming Byron Gottfried - THM

IM - 401 Image Processing

Syllabus to be offered at M. Sc. Industrial Mathematics Sem -IV w.e.f. June 2011-12

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Introduction

Fundamentals of Image Processing, Applications of Image Processing, Automatic Visual Inspection System, Remotely Sensed Scene Interpretation, Biomedical Imaging Techniques, Defense surveillance, Content-Based Image Retrieval, Moving-Object Tracking, Image and Video Compression, Human Visual Perception, Human Eyes, Neural Aspects of the Visual Sense, Components of an Image Processing System, Digital Camera

Image Formations and Representation

Introduction, Image formation, Illumination, Reflectance Models, Point Spread Function, Sampling and Quantization, Image Sampling, Image Quantization, Binary Image, Geometric Properties, Chain code representation of a binary object, Three-Dimensional Imaging, Stereo Images, Range Image Acquisition, Image file formats

Colors and Color Imagery

Introduction, Perception of Colors, Color Space Quantization and Just Noticeable Difference, Color Space and Transformation, CMYK, NTSC or YIQ Color, YCbCr Color, Perceptually Uniform Color, CIELAB color, Color Interpolation or Demosaicing, Nonadaptive Color Interpolation Algorithms, Adaptive algorithms, A Novel Adaptive Color Interpolation Algorithm,

Image Transformations

Introduction, Fourier Transforms, One-Dimensional Fourier Transform, Two-Dimensional Fourier Transform, Discrete Fourier Transform (DFT), Transformation Kernels, Matrix Form Representation, Properties, Fast Fourier Transform, Discrete Cosine Transform, Walsh-Hadamard Transform (WHT), Karhunen-Loeve Transform or Principal Component Analysis, Covariance Matrix, Eigenvectors and Eigenvalues, Principal Component Analysis, Singular Value Decomposition

References:

1. Tinku Acharya & Ajoy K. Ray, 'Image Processing ,Principles and Applications' WILEY-INTERSCIENCE
2. Gonzalez & Woods, "Digital image processing" Pearson Education second edition

IM - 402 Wavelet Analysis

Syllabus to be offered at M. Sc. Industrial Mathematics Sem -IV w.e.f. June 2011-12

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- From Fourier Analysis to Wavelet analysis
- Time Frequency Analysis
- Continuous Wavelet Transform
- Discretizing the Wavelet Transform
- Frames
- Frames of Wavelets
- A necessary condition (Admissibility of the mother wavelet)
- The dual frame
- Examples of Tight frames, The Mexican hat function, a modulated Gaussian
- Frames for the Windowed Fourier transform
- Time-Frequency Density
- Orthonormal Wavelet bases
- Multi Resolution Analysis
- Riesz bases of scaling function
- The Battle-Lemaire wavelets
- Regularity of Orthonormal wavelet bases
- Orthonormal Bases of Compactly Supported Wavelets with Examples
- Regularity of Compactly Supported Wavelets

References:

1. Ingrid Daubechies :Ten Lectures on Wavelets, OBMS-NSF SIAM, Philadelphia, 1992.
2. Charles K. Chui An introduction to wavelets, Academic Press ,1992
3. G. Kaiser, Friendly Guide to wavelets , Birkhauser Boston 1994.

IM 403: Digital Signal Processing

Syllabus to be offered at M. Sc. Industrial Mathematics Sem -IV w.e.f. June 2011-12

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INTRODUCTION:

DISCRETE-TIME SIGNALS AND SYSTEMS:

Introduction, Discrete-Time Signals: Sequences, Discrete-Time systems, Linear Time-Invariant Systems, Properties of Linear Time-Invariant Systems, Linear Constant-Coefficient Difference Equations, Frequency-Domain Representation of Discrete-Time Signals and Systems, Representation of Sequences by Fourier Transforms, Symmetry Properties of the Fourier Transform, Fourier Transform Theorems, Discrete-Time Random Signals.

THE Z-TRANSFORM:

Introduction, Z-Transform, Properties of the Region of Convergence for the Z-Transform, The Inverse Z-Transform, Z-Transform Properties.

SAMPLING OF CONTINUOUS - TIME SIGNALS:

Introduction, Periodic Sampling, Frequency-Domain Representation of Sampling, Reconstruction of a Bandlimited Signal from its Samples, Discrete-Time Processing of Continuous-Time Signals, Continuous-Time Processing of Discrete-Time Signals, Changing the Sampling Rate Using Discrete-Time Processing, Multirate Signal Processing, Digital Processing of Analog Signals, Oversampling and Noise Shaping in A/D and D/A Conversion.

TRANSFORM ANALYSIS OF LINEAR TIME-INVARIANT SYSTEMS:

Introduction, The Frequency Response of LTI Systems, System Functions for Systems Characterized by Linear constant-coefficient Difference Equations, Frequency Response for Rational System Functions, Relationship between Magnitude and Phase, All-Pass Systems, Minimum Phase Systems, Linear Systems with Generalized Linear Phase.

References:

1. oppenheim A. V., Schafer & Buck "Discrete Time Signal Processing" Pearson education 2006
2. crochiere & rabiner "multirate Digital Signal Processing" Pearson education 2006
3. oppenheim A. V., Schafer, "Digital Signal Processing" Pearson education 2006

IM 404: Computational Fluid Dynamics

Syllabus to be offered at M. Sc. Industrial Mathematics Sem -IV w.e.f. June 2011-12

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- Introduction to CFD, Applications;
- Governing equations and assumptions, Equation types, Model equations, potential flow, Heat conduction, Wave equation, Burgers equation, Euler equations.
- Finite Differences, Algorithms, Errors and Accuracy, Consistency, Stability and Convergence, Finite Volumes, Explicit algorithms, Implicit algorithms, Numerical boundary conditions, Method of lines, Shock Jump Relations, Shock capturing.
- One dimensional Euler equations, Lax – Wendroff Scheme, Mc-Cormack Scheme, Implicit - method, Pseudo One Dimensional Euler Equations, boundary conditions, Flux – Splitting, Artificial viscosity, Flux limiters.
- Multidimensional Euler equations, Lax- Wendroff and Mc-Cormack schemes, stability of multidimensional schemes, Operator splitting Implicit algorithms, Beam - Warming algorithm.
- Practicals : Numerical methods for discretizing fluid flow equations: Finite differences, finite element and finite volume method.

References:

1. R. J. Leveque: Numerical methods for conservation Laws, Birkhauser Verlag, Basel, 1992.
2. J. D. Anderson: Computation Fluid dynamics, Mc-Graw – Hill, New York, 1995.
3. H. K. Versteeg and W. Malasekera: An Introduction to Computational Fluid Dynamics: The finite volume method, Longman Scinetific and technical Essex, England, 1995.
4. J. Chorin and J. E. Marsden: A Mathematical Introduction to Fluid Mechanics
5. P. D. Lax: hyperbolic systems of conservation laws and mathematical theory of shock waves, 1973.

IM 405: Neural Network

Syllabus to be offered at M. Sc. Industrial Mathematics Sem -IV w.e.f. June 2011-12

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Definition and brief history of artificial neural networks.

- Structure and function of a Single Neuron, Biological Neuron and artificial Neuron Models
- Architectures and Neural Networks:
 - Fully connected
 - Layered networks
 - Feed forward
 - A cyclic and modular networks
- Supervized and Unsupervised networks
- Learning Algorithms:
 - Correlation learning
 - Competitive learning
 - Habbian rule
 - Perceptron rule
 - Delta rule
 - Back propagation algorithm.
- Hopfield Networks
 - Continuous and Discrete
 - Energy function and its properties
 - Capacity of Hopfield Networks.
- Radial Basis Function Networks, Cover's theorem.
- Application of Neural Networks
 - Classification
 - Clustering

- Pattern association
- Function Approximation
- Forecasting
- Control application
- Optimization

References:

1. Heykin S: Neural Networks : A Comprehensive Foundation, McMillan, N.Y, 1994
2. Kohonen. T: Self-Organization and Associative Memory.
3. Kosko B: Neural Networks and Fuzzy Systems : Prentice Hall, Y.J, 1992.
4. K Mehrotra, C.K. Mohan, S. Ranka : Artificial Neural Networks, Penram International Publishing, 1977.

IM 406: Mathematical Software

Syllabus to be offered at M. Sc. Industrial Mathematics Sem -IV w.e.f. June 2011-12

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Introduction

Introduction to Matlab, variable and array, subarrays, displaying output data, data files operation on array, hierarchy of operation on array, built in function in Matlab

Plotting

Introduction to plotting, graph window, two dimensional plot, multiple plot, components of graph(legend, title,), graphical image, comment, 3D graph, additional plotting features
Subplots, polar plots,

Branching statement and program design

The if construct, switch construct, The try-catch construct , relational operators, logic operators, logical functions

Loops

The while loop, The for loop, The break and continue statements, Nesting loops.

User defined function

Introduction to Matlab functions, variable passing in Matlab(pass by value), preserving data between calls to functions, sub functions, private function, nested function

Practical based on image processing, wavelet, digital signal processing, neural network

References:

1. Chapman Stephen: Matlab programming for engineers, Thompson learning, 2004.
2. Rudra Pratap: getting started with Matlab, oxford university press, 2004